3.6 Introduction to trigonometry

Figure 3.8 shows two triangles whose angles are the same but the lengths of whose sides vary. In order that the angles remain the same the lengths of the corresponding sides must vary in the same ratio as shown.

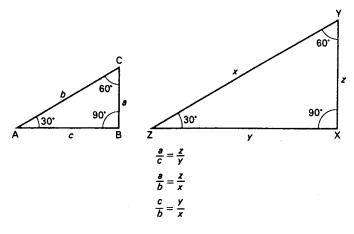


Fig. 3.8 Similar triangles

It can be seen, therefore, that the size of the acute angles in any right-angled triangle can be stated as the ratio of any two of the sides. Figure 3.9 shows a right-angled triangle and shows how the sides of the triangle are named.

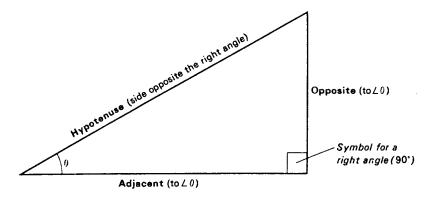


Fig. 3.9 The sides of the right-angled triangle

The ratios of these sides for a given angle are given special names as shown in Fig. 3.10. They are called the *trigonometrical ratios*. To keep things simple only the right-angled triangle will be considered in this chapter, and for most workshop purposes this is sufficient. At a more advanced level, trigonometry can be applied to any sort of triangle and angles of any magnitude.

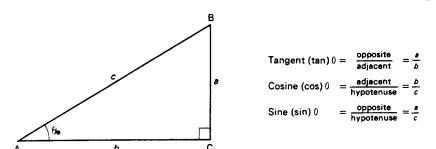


Fig. 3.10 The trigonometrical ratios

3.7 Trigonometrical tables

These are used to evaluate problems involving the sides and angles of triangles (trigonometry). Tables of natural tangents, natural sines, and natural cosines are included at the end of this book. Trigonometrical tables are used in a similar manner to the tables of logarithms introduced in *Basic Engineering*. Figures 3.11 to 3.13 inclusive show how the tables should be read. Figures 3.14 to 3.16 give examples involving the use of trigonometry.

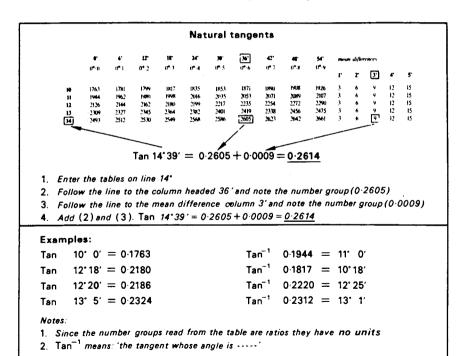


Fig. 3.11 Reading tables of natural tangents

Natural sines 119.4 5075 5105 5120 Suis 980 5135 5150 5299 5165 5190 5195 5210 5225 5240 5255 5270 5784 5314 5129 5373 5388 5417 4344 510 5407 433 5446 5461 5406 5577 -5534 554X 5563 Seem 5505 5519 5707 Sin 34.17 = 0.5621 + 0.0012 = 0.5633

- 1. Enter the tables on line 34°
- 2. Follow the line to the column headed 12' and note the number group (0.5621)
- 3. Follow the line to the mean difference column 5' and note the number group (0.0012)
- 4. Add (2) and (3). Sin $34^{\circ}17' = 0.5621 + 0.0012 = \underline{0.5633}$

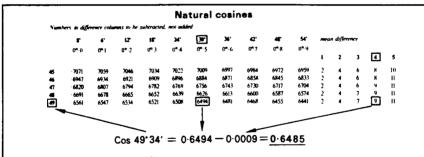
Examples:

Sin	30° 0′ = 0·5000	Sin ⁻¹	0.5150	=	31°	0,
Sin	$31^{\circ}30' = 0.5225$	Sin ⁻¹	0.5388	=	32°3	36′
Sin	$32^{\circ}45' = 0.5409$	Sin ⁻¹	0.5558	=	33°4	16′
Sin	33° 1′ = 0.5448	Sin ⁻¹	0.5594	=	34"	1′

Notes:

- 1. Since the number groups read from the table are ratios they have no units
- 2. Sin-1 means: 'the sine whose angle is -----'

Fig. 3.12 Reading tables of natural sines



- 1. Enter the tables on line 49°
- 2. Follow the line to the column headed 30' and note the number group (0.6494)
- 3. Follow the line to the mean difference column 4' and note the number group (0.0009)
- 4. SUBTRACT (3) from (2). Cos $49^{\circ}34' = 0.6494 0.0009 = 0.6485$

Examples:

Cos
$$46^{\circ}$$
 0' = 0.6947
 \cos^{-1} 0.6820 = 47° 0'

Cos
 45° 24' = 0.7022
 \cos^{-1} 0.6934 = 46° 6'

Cos
 48° 47' = 0.6589
 \cos^{-1} 0.6780 = 47°17'

Cos
 47° 2' = 0.6816
 \cos^{-1} 0.6680 = 48° 5'

Notes

- 1. Since the number groups read from the tables are ratios they have no units
- 2. Cos-1 means: 'the cosine whose angle is -----'

Fig. 3.13 Reading tables of natural cosines

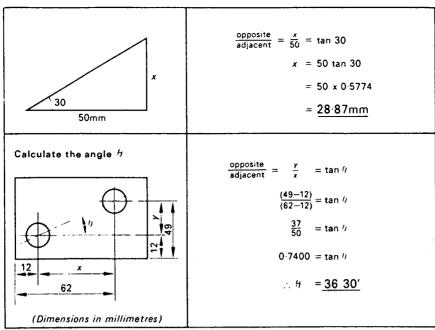


Fig 3.14 Use of trigonometry - tangents

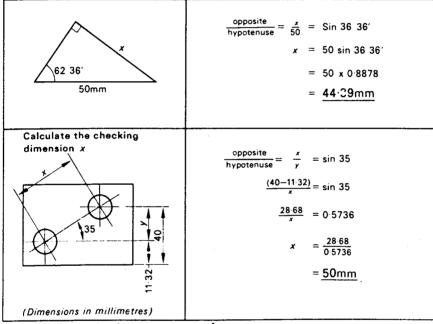


Fig 3.15 Use of trigonometry - sines

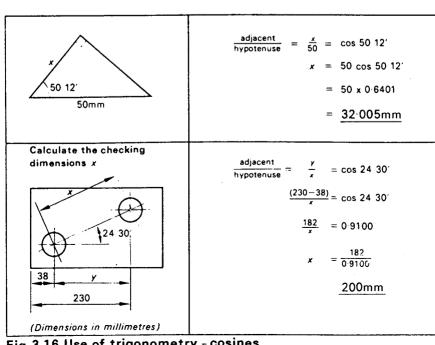


Fig 3.16 Use of trigonometry - cosines

Natural sines

Degrees	0 ′	6' 0 ·1	12' 0 ·2	18′ 0 ·3	24' 0 4	30′ 0 ·5	36 ′ 0 ·6	42' 0 ·7	48′ 0∵8	54′ 0 ·9		Di	Me: fere	n ence	
Deg						0.0	0.0		0 0	0 3	1	2	3	4	5
0	-0000	0017	0035	0052	0070	0087	0105	0122	0140	0157	3	6	9	12	15
1	∙0175	0192	0209	0227	0244	0262	0279	0297	0314	0332	3	6	9	12	15
2	0349	0366	0384	0401	0419	0436	0454	0471	0488	0506	3	6	9	12	15
3	∙0523	0541	0558	.0576	0593	0610	0628	0645	0663	0680	3	6	9	12	15
4	∙0698	0715	0732	0750	0767	0785	0802	0819	0837	0854	3	6	9	12	15
5	∙0872	0889	0906	0924	0941	0958	0976	0993	1011	1028	3	6	9	12	14
6	·1045	1063	1080	1097	1115	1132	1149	1167	1184	1201	3	6	9	12	14
7	1219	1236	1253	1271	1288	1305	1323	1340	1357	1374	3	6	9	12	14
8	·1392	1409	1426	:1444	1461	1478	1495	1513	1530	1547	3	6	9	12	14
9	∙1564	1582	1599	1616	1633	1650	1668	1685	1702	1719	3	6	9	12	14
10	⋅1736	1754	1771	1788	1805	1822	1840	1857	1874	1891	3	6	9	12	14
11	1908	1925	1942	1959	1977	1994	2011	2028	2045	2062	3	6	9	11	14
12	⋅2079	2096	2113	2130	2147	2164	2181	2198	2215	2232	3	6	9	11	14
13	·2250	2267	2284	2300	2317	2334	2351	2368	2385	2402	3	6	8	11	14
14	·2419	2436	2453	2470	2487	2504	2521	2538	2554	2571	3	6	8	11	14
15	2588	2605	2622	2639	2656	2672	2689	2706	2723	2740	3	6	8	11	14
16	2756	2773	2790	2807	2823	2840	2857	2874	2890	2907	3	6	8	11	14
17	2924	2940	2957	2974	2990	3007	3024	3040	3057	3074	3	6	8	11	14
18	-3090	3107	3123	3140	3156	3173	3190	3206	3223	3239	3	6	8	11	14
19	·3256	3272	3289	3305	3322	3338	3355	3371	3387	3404	3	5	8	11	14
20	·3420	3437	3453	3469	3486	3502	3518	3535	3551	3567	3	5	8	11	14
21	·3584	3600	3616	3633	3649	3665	3681	3697	3714	3730	3	5	8	11	14
22	·3746	3762	3778	3795	3811	3827	3843	3859	3875	3891	3	5	8	11	14
23	·3907	3923	3939	3955	3971	3987	4003	4019	4035	4051	3	5	8	11	14
24	4067	4083	4099	4115	4131	4147	4163	4179	4195	4210	3	5	8	11	13
25	·4226	4242	4258	4274	4289	4305	4321	4337	4352	4368	3	5	8	11	13
26	4384	4399	4415	4431	4446	4462	4478	4493	4509	.4524	3	5	8	10	13
27	·4540	4555	4571	4586	4602	4617	4633	4648	4664	4679	3	5	8	10	13
28	·4695	4710	4726	4741	4756	4772	4787	4802	4818	4833	3	5	8	10	13
29	·4848	4863	4879	4894	4909	4924	4939	4955	4970	4985	3	5	8	10	13
30	·5000	5015	5030	5045	5060	5075	5090	5105	5120	5135	3	5	8	10	13
31	·5150	5165	5180	5195	5210	5225	5240	5255	5270	5284	2	5	7	10	12
32	∙5299	5314	5329	5344	5358	5373	5388	5402	5417	5432	2	5	7	10	12
33	·5446	5461	5476	5490	5505	5519	5534	5548	5563	5577	2	5	7	10	12
34	·5592	5606	5621	5635	5650	5664	5678	5693	5707	5721	2	5	7	10	12
35	5736	5750	5764	5779	5793	5807	5821	5835	5850	5864	2	5	7	10	12
36	5878	5892	5906	5920	5934	5948	5962	5976	5990	6004	2	5	7	9	12
37	6018	6032	6046	6060	6074	6088	6101	6115	6129	6143	2	5	7		12
38	6157	6170	6184	6198	6211	6225	6239	6252	6266	6280	2	5	7		11
39	6293	6307	6320	6334	6347	6361	6374	6388	6401	6414	2	4	7	9	11
40	6428	6441	6455	6468	6481	6494	6508	6521	6534	6547	2	4	7		11
41	6561	6574	6587	6600	6613	6626	6639	6652	6665	6678	2	4	7		11
42	6691	6704	6717	6730	6743	6756	6769	6782	6794	6807	2	4	6	-	11
43	6820	6833	6845	6858	6871	6884	6896	6909	6921	6934	2	4	6		11
44	6947	6959	6972	6984	6997	7009	7022	7034	7046	7059	2	4	6	8	10

Natural sines

	1	Т-					,	_			, -				
Degrees	0′	6′	12′	18′	24	30´	36 ′	42'	48′	54		D:	Mea		
egr.	0.0	0 ·1	0 .2	0 .3	0 4	0 .5	0.6	0 7	0 .8	0 .9			ffere	T	
ă		L									1	2	3	4	5
45	7071	7083	7096	7108	7120	7133	7145	7157	7169	7181	2	4	6	8	10
46	·7193	7206	7218	7230	7242	7254	7266	7278	7290	7302	2	4	6	8	10
47	-7314	7325	7337	7349	7361	7373	7385	7396	7408	7420	2	4	6	8	10
48	·7431	7443	7455	7466	7478	7490	7501	7513	7524	7536	2	4	6	8	10
49	7547	7558	7570	7581	7593	7604	7615	7627	7638	7649	2	4	6	8	9
50	.7660	7672	7683	7694	7705	7716	7727	7738	7749	7760	2	4	6	7	9
51	7771	7782	7793	7804	7815	7826	7837	7848	7859	7869	2	4	5	7	9
52	·7880	7891	7902	7912	7923	7934	7944	7955	7965	7976	2	4	5	7	9
53	7986	7997	8007	8018	8028	8039	8049	8059	8070	8080	2	3	5	7	9
54	-8090	8100	8111	8121	8131	8141	8151	8161	8171	8181	2	3	5	7	8
55	-8192	8202	8211	1	İ				1		1			-	
56	8290	8300	8310	8221	8231	8241	8251	8261	8271	8281	2	3	5	7	8
57	8387	8396	8406	8320	8329	8339	8348	8358	8368	8377	2	3	5	6	8
58	-8480	8490	8499	8415	8425	8434	8443	8453	8462	8471	2	3	5	6	8
59	8572	8581	8590	8508 8599	8517	8526	8536	8545	8554	8563	2	3	5	6	8
	ł				8607	8616	8625	8634	8643	8652	1	3	4	6	7
60	·8660	8669	8678	8686	8695	8704	8712	8721	8729	8738	1	3	4	6	7
61	·8746	8755	8763	8771	8780	8788	8796	8805	8813	8821	1	3	4	6	7
62	-8829	8838	8846	8854	8862	8870	8878	8886	8894	8902	1	3	4	5	7
63	-8910	8918	8926	8934	8942	,8949	8957	8965	8973	8980	1	3	4	5	6
64	-8988	8996	9003	9011	9018	9026	9033	9041	9048	9056	1	3	4	5	6
65	· 906 3	9070	9078	9085	9092	9100	9107	9114	9121	9128	1	2	4	5	6
66	9135	9143	9150	9157	9164	9171	9178	9184	9191	9198	ī	2	3	5	6
67	∙9205	9212	9219	9225	9232	9239	9245	9252	9259	9265	1	2	3	4	6
68	·9272	9278	9285	9291	9298	9304	9311	9317	9323	9330	1	2	3	4	5
69	∙9336	9342	9348	9354	9361	9367-	9373	9379	9385	9391	1	2	3	4	5
70	.9397	9403	9409	9415	9421	9426	9432	9438	9444	9449	1	2	3	4	5
71	9455	9461	9466	9472	9478	9483	9489	9494	9500	9505	1	2	3	4	5
72	9511	9516	9521	9527	9532	9537	9542	9548	9553	9558	1	2	3	3	4
73	9563	9568	9573	9578	9583	9588	9593	9598	9603	9608	î	2	2	3	4
74	-9613	9617	9622	9627	9632	9636	9641	9646	9650	9655	1	2	2	3	4
75	·9659	9664	9668	9673	9677	9681	9686	9690	9694	0000	١.		_		
76	9703	9707	9711	9715	9720	9724	9728	9732	9736	9699 9740	1	1	2	3	4
77	.9744	9748	9751	9755	9759	9763	9767	9770	9774	9778	1	1	2	3	3 3
78	9781	9785	9789	9792	9796	9799	9803	9806	9810	9813	1	1	2	2	3
79	·9816	9820	9823	9826	9829	9833	9836	9839	9842	9845	1	1	2	2	3
						!		1						_	
80	·9848	9851	9854	9857	9860	9863	9866	9869	9871	9874	0	1	1	2	2
81	·9877	9880	9882	9885	9888	9890	9893	9895	9898	9900	0	1	1	2	2
82 83	·9903 ·9925	9905 9928	9907 9930	9910	9912	9914	9917	9919	9921	9923	0	1	1	2	2
84	9945	9947	9949	9932 9951	9934 9954	9936	9938	9940	9942	9943	0	1	1	1	2
						9954	9956	9957	9959	9960	0	1	1	. 1	2
85	9962	9963	9965	9966	9968	9969	9971	9972	9973	9974	0	0	1	1	1
86	9976	9977	9978	9979	9980	9981	9982	9983	9984	9985	0	0	1	1	1
87	9986	9987	9988	9989	9990	9990	991	9992	9993	9993	0	0	0	1	1
88	·9994	9995	9995	9996	9996	9997	9997	9997	9998	9998	0	0	0	0	0
89	9998	9999	9999	9999	9999	1.000	1.000	1.000	1.000	1.000	0	0	0	0	0
90	1.000														
								لــــا			_				

Natural cosines

Numbers in difference columns to be subtracted, not added

ees	0 ′ 0′	6′ 0°⋅1	12′ 0°.2	18′ 0°-3	24′ 0°·4	30 ′ 0°-5	36 ′ 0°-6	42′ 0 ·7	48′ 0∴8	54 ′ 0∵9			Mea Terei		
Degrees	0 0	0 1	0 2			0 0			•		1	2	3	4	5
0	1.000	1.000	1.000	1.000	1.000	1.000	-9999	9999	9999	9999	0	0	0	0	0
1	-9998	9998	9998	9997	9997	9997	9996	9996	9995	9995	0	0	0	0	0
2	9994	9993	9993	9992	9991	9990	9990	9989	9988	9987	0	0	0	1	1
3	9986	9985	9984	9983	9982	9981	9980	9979	9978	9977	0	0	1	1	1
4	∙9976	9974	9973	9972	9971	9969	9968	9966	9965	9963	0	0	1	1	1
5	·9962	9960	9959	9957	9956	9954	9952	9951	9949	9947	0	1	1	1	2
6	·9945	9943	9942	9940	9938	9936	9934	9932	9930	9928	0	1	1	1	2
7	·9925	9923	9921	9919	9917	9914	9912	9910	9907	9905	0	1	1	2	2
8	-9903	9900	9898	9895	9893	9890	9888	9885	9882	9880	0	1	1	2	2
9	9877	9874	9871	9869	9866	9863	9860	9857	9854	9851	0	1	1	2	2
10	9848	9845	9842	9839	9836	9833	9829	9826	9823	9820	1	1	2	2	3
11	-9816	9813	9810	9806	9803	9799	9796	9792	9789	9785	1	1	2	2	3
12	.9781	9778	9774	9770	9767	9763	9759	9755	9751	9748	1	1	2	3	3
13	·9744	9740	9736	9732	9728	9724	9720	9715	9711	9707	1	1	2	3	3
14	∙9703	9699	9694	9690	9686	9681	9677	9673	9668	9664	1	1	2	3	4
15	-9659	9655	9650	9646	9641	9636	9632	9627	9622	9617	1	2	2	3	4
16	·9613	9608	9603	9598	9593	9588	9583	9578	9573	9568	1	2	2	3	4
17	9563	9558	9553	9548	9542	9537	9532	9527	9521	9516	1	2	3	3	4
18	·9511	9505	9500	9494	9489	9483	9478	9472	9466	9461	1	2	3	4	5
19	-9455	9449	9444	9438	9432	9426	9421	9415	9409	9403	1	2	3	4	5
20	-9397	9391	9385	9379	9373	9367	9361	9354	9348	9342	1	2	3	4	5
21	9336	9330	9323	9317	9311	9304	9298	9291	9285	9278	1	2	3	4	5
22	-9272	9265	9259	9252	9245	9239	9232	9225	9219	9212	1	2	3	4	6
23	∙9205	9198	9191	9184	9178	9171	9164	9157	9150	9143	1	2	3	5	6
24	∙9135	9128	9121	9114	9107	9100	9092	9085	9078	9070	1	2	4	5	6
25	-9063	9056	9048	9041	9033	9026	9018	9011	9003	8996	1	3	4	5	6
26	·8988	8980	8973	8965	8 9 57	8949	8942	8934	8926	8918	1	3	4	5	6
27	·8910	8902	8894	8886	8878	8870	8862	8854	8846	8838	1	3	4	5	7
28	⋅8829	8821	8813	8805	8796	8788	8780	8771	8763	8755	1	3	4	6	7
29	⋅8746	8738	8729	8721	8712	8704	8695	8686	8678	8669	1	3	4	6	7
30	-8660	8652	8643	8634	8625	8616	8607	8599	8590	8581	1	3	4	6	7
31	-8572	8563	8554	8545	8536	8526	8517	8508	8499	8490	2	3	5	6	8
32	-8480	8471	8462	8453	8443	8434	8425	8415	8406	8396	2	3	5	6	8
33	-8387	8377	8368	8358	8348	8339	8329	8320	8310	8300	2	3	5	6	8
34	⋅8290	8281	8271	8261	8251	8241	8231	8221	8211	8202	2	3	5	7	8
35	8192	8181	8171	8161	8151	8141	8131	8121	8111	8100	2	3	5	7	8
36	-8090	8080	8070	8059	8049	8039	8028	8018	8007	7997	2	3	5	7	9
37	7986	7976	7965	7955	7944	7934	7923	7912	7902	7891	2	4	5	7	9
38	·7880	7869	7859	7848	7837	7826	7815	7804	7793	7782	2	4	5	7	9
39	·7771	7760	7749	7738	7727	7716	7705	7694	7683	7672	2	4	6	7	9
40	-7660	7649	7638	7627	7615	7604	7593	7581	7570	7559	2	4	6	8	9
41	·7547	7536	7524	7513	7501	7490	7478	7466	7455	7443	2	4	6	8	10
42	·7431	7420	7408	7396	7385	7373	7361	7349	7337	7325	2	4	6	8	10
43	·7314	7302	7290	7278	7266	7254	7242	7230	7218	7206	2	4	6		10
44	·7193	7181	7169	7157	7145	7133	7120	7108	7096	7083	2	4	6	8	10
	L					1	L	L		ı	_			ь	_

Natural cosines

rees	0 ′ 0`-0	6′ 0°·1	12' 0 ·2	18' 0 ·3	24' 0 ·4	30 ′ 0 ·5	36 ′ 0 ·6	42 ′ 0 ·7	48 ′ 0∵8	54 ′ 0∵9		Di	Mea	an ences
Degrees			0 2	0.3	0 4	0.3	0.8	0 1	0.9	0.9	1	2	3	4 5
45	·7071	7059	7046	7034	7022	7009	6997	6984	6972	6959	2	4	6	8 10
46	-6947	6934	6921	6909	6896	6884	6871	6858	6845	6833	2	4	6	8 11
47	-6820	6807	6794	6782	6769	6756	6743	6730	6717	6704	2	4	6	9 11
48	·6691	6678	6665	6652	6639	6626	6613	6600	6587	6574	2	4	7	9 11
49	6561	6547	6534	6521	6508	6494	6481	6468	6455	6441	2	4	7	9 11
50	-6428	6414	6401	6388	6374	6361	6347	6334	6320	6307	2	4	7	9 11
51	-6293	6280	6266	6252	6239	6225	6211	6198	6184	6170	2	5	7	9 11
52	·6157	6143	6129	6115	6101	6088	6074	6060	6046	6032	2	5	7	9 12
53	6018	6004	5990	5976	5962	5948	5934	5920	5906	5892	2	5	7	9 12
54	-5878	5864	5850	5835	5821	5807	5793	5779	5764	5750	2	5	7	9 12
55	-5736	5721	5707	5693	5678	5664	5650	5635	5621	5606	2	5	7	10 12
56	-5592	5577	5563	5548	5534	5519	5505	5490	5476	5461	2	5	7	10 12
5 7	∙5446	5432	5417	5402	5388	5373	5358	5344	5329	5314	2	5	7	10 12
58	-5299	5284	5270	5255	5240	5225	5210	5195	5180	5165	2	5	7	10 12
59	∙5150	5135	5120	5105	5090	5075	5060	5045	5030	5015	3	5	8	10 13
60	-5000	4985	4970	4955	4939	4924	4909	4894	4879	4863	3	5	8	10 13
61	·4848	4833	4818	4802	4787	4772	4756	4741	4726	4710	3	5	8	10 13
62	·4695	4679	4664	4648	4633	4617	4602	4586	4571	4555	3	5	8	10 13
63	∙4540	4524	4509	4493	4478	4462	4446	4431	4415	4399	3	5	8	10 13
64	·4384	4368	4352	4337	4321	4305	4289	4274	4258	4242	3	5	8	11 13
65	·4226	4210	4195	4179	4163	4147	4131	4115	4099	4083	3	5	8	11 13
66	4067	4051	4035	4019	4003	3987	3971	3955	3939	3923	3	5	8	11 14
67	-3907	3891	3875	3859	3843	3827	3811	3795	3778	3762	3	5	8	11 14
68	·3746	3730	3714	3697	3681	3665	3649	3633	3616	3600	3	5	8	11 14
69	∙3584	3567	3551	3535	3518	3502	3486	3469	3453	3437	3	5	8	11 14
70	-3420	3404	3387	3371	3355	3338	3322	3305	3289	3272	3	5	8	11 14
71	3256	3239	3223	3206	3190	3173	3156	3140	3123	3107	3	6	8	11 14
72	·3090	3074	3057	3040	3024	3007	2990	2974	2957	2940	3	6	8	11 14
73	2924	2907	2890	2874	2857	2840	2823	2807	2790	2773	3	6	8	11 14
74	2756	2740	2723	2706	2689	2672	2656	2639	2622	2605	3	6	8	11 14
75	2588	2571	2554	2538	2521	2504	2487	2470	2453	2436	3	6	8	11 14
76	·2419	2402	2385	2368	2351	2334	2317	2300	2284	2267	3	6	8	11 14
77	·2250	2233	2215	2198	2181	2164	2147	2130	2113	2096	3	6	9	11 14
78	·2079	2062	2045	2028	2011	1994	1977	1959	1942	1925	3	6	9	11 14
79	1908	1891	1874	1857	1840	1822	1805	1788	1771	1754	3	6	9	11 14
80	·1736	1719	1702	1685	1668	1650	1633	1616	1599	1582	3	6	9	12 14
81	·1564	1547	1530	1513	1495	1478	1461	1444	1426	1409	3	6	9	12 14
82	·1392	1374	1357	1340	1323	1305	1228	1271	1253	1236	3	6	9	12 14
83	·1219	1201	1184	1167	1149	1132	1115	1097	1080	1063	3	6	9	12 14
84	·1045	1028	1011	0993	0976	0958	0941	0924	0906	0889	3	6	9	12 14
85	·0872	0854	0837	0819	0802	0785	0767	0750	0732	0715	3	6	9	12 15
86	.0698	0680	0663	0645	0628	0610	0593	0576	0558	0541	3	6	9	12 15
87	0523	0506	0488	0471	0454	0436	0419	0401	0384	0366	3	6	9	12 15
88	.0349	0332	0314	0297	0279	0262	0244	0227	0209	0192	3	6	9	12 15
89	.0175	0157	0140	0122	0105	0087	0070	0052	0035	0017	3	6	9	12 15
90	0000							l						
										·				

Natural tangents

899	0 ′ 0°∙0	6′	12′ 0°.2	18′ 0°·3	24′	30 ′	36′	42′	48′	54′	N	dean.	Diffe	rence	:8
Degrees	0.0	0°∙1	0°.2	0°.3	0°-4	0°.5	0°·6	0°.7	0°.8	0∵9	1	2	3	4	5
0	·0000	0017	0035	0052	0070	0087	0105	0122	0140	0157	3	6	9	12	15
1	0175	0192	0209	0227	0244	0262	0279	0297	0314	0332	3	6	9	12	15
2	0349	0367	0384	0402	0419	0437	0454	0472	0489	0507	3	6	9	12	15
3	0524	0542	0559	0577	0594	0612	0629	0647	0664	0682	3	6	9	12	15
4	·0699	0717	0734	0752	0769	0787	0805	0822	0840	0857	3	6	9	12	15
5	∙0875	0892	0910	0928	0945	0963	0981	0998	1016	1033	3	6	9	12	15
6	·1051	1069	1086	1104	1122	1139	1157	1175	1192	1210	٤	6	9	12	15
7	·1228	1246	1263	1281	1299	1317	1334	1352	1370	1388	3	6	9	12	15
8	·1405	1423	1441	1459	1477	1495	1512	1530	1548	1566	3	6	9	12	15
9	·1584	1602	1620	1638	1655	1673	1691	1709	1727	1745	3	6	9	12	15
10	·1763	1781	1799	1817	1835	1853	1871	1890	1908	1926	3	6	9	12	15
11	∙1944	1962	1980	1998	2016	2035	2053	2071	2089	2107	3	6	9	12	15
12	2126	2144	2162	2180	2199	2217	2235	2254	2272	2290	3	6	9	12	15
13	2309	2327	2345	2364	2382	2401	2419	2338	2456	2475	3	6	9	12	15
14	2493	2512	2530	2549	2568	2586	2605	2623	2642	2661	3	6	9	12	16
15	2679	2698	2717	2736	2754	2773	2792	2811	2830	2849	3	6	9	13	16
16	2867	2886	2905	2924	2943	2962	2981	3000	3019	3038	3	6	9	13	16
17	3057	3076	3096	3115	3134	3153	3172	3191	3211	3230	3	6	10	13	16
18	·3249	3269	3288	3307	3327	3346	3365	3385	3404	3424	3	6	10	13	16
19	·3443	3463	3482	3502	3522	3541	3561	3581	3600	3620	3	7	10	13	16
20	·3640	3659	3679	3699	3719	3739	3759	3779	3799	3819	3	7	10	13	17
21	3839	3895	3879	3899	3919	3939	3959	3979	4000	4020	3	7	10	13	17
22	· 4 040	4061	4081	4101	4122	4142	4163	4183	4204	4224	3	7	10	14	17
23	·4245	4265	4286	4307	4327	4348	4369	4390	4411	4431	3	7	10	14	17
24	·4452	4473	4494	4515	4536	4557	4578	4599	4621	4642	4	7	11	14	18
25	4663	4684	4706	4727	4748	4770	4791	4813	4834	4856	4	7	11	14	18
26	·4877	4899	4921	4942	4964	4986	5008	5029	5051	5073	4	7	11	15	18
27	∙5095	5117	5139	5161	5184	5206	5228	5250	5272	5295	4	7	11	15	18
28	·5317	5340	5362	5384	5407	5430	5452	5475	5498	5520	4	8	11	15	19
29	.5543	5566	5589	5612	5635	5658	5681	5704	5727	5750	4	8	12	15	19
30	.5774	5797	5820	5844	58€7	5890	5914	5938	5961	5985	4	8	12	16	20
31	-6009	6032	6056	6080	6104	6128	6152	6176	6200	6224	4	8	12	16	20
32	-6249	6273	6297	6322	6346	6371	6395	6420	6445	6469	4	8	12	16	20
33	6494	6519	6544	6569	6594	6619	6644	6669	6694	6720	4	8	13	17	21
34	6745	6771	6796	6822	6847	6873	6899	6924	6950	6976	4	9	13	17	21
35	7002	7028	7054	7080	7107	7133	7159	7186	7212	7239	4	9	13	18	22
36	·7265	7292	7319	7346	7373	7400	7427	7454	7481	7508	5	9	14	18	23
37	·7536	7563	7590	7618	7646	7673	7701	7729	7757	7785	5	9	14	18	23
38	7813	7841	7869	7898	7926	7954	7983	8012	8040	8069	5	9	14	19	24
39	-8098	8127	8156	8185	8214	8243	8273	8302	8332	8361	5	10	15	20	24
40	·8391	8421	8451	8481	8511	8541	8571	8601	8632	8662	5	10	15	20	25
41	·8 69 3	8724	8754	8785	8816	8847	8878	8910	8941	8972	5	10	16	21	26
42	-9004	9036	9067	9099	9131	9163	9195	9228	9260	9293	5	11	16	21	27
43	9325	9358	9391	9424	9457	9490	9523	9556	9590	9623	6	11	17	22	28
44	-9657	9691	9725	9759	9793	9827	9861	9896	9930	9965	6	11	17	23	29

Natural tangents

		T	ī			Γ	T		_						
Degrees	0.0	6' 0"-1	12' 0' 2	18′ 0°·3	24' 0'4	30 ′ 0°.5	36 ′ 0°.6	42′ 0°·7	48′ 0′-8	54 ′ 0°.9	L	Mea	n Diff	erend	es
مَّ											1	2	3	4	5
45	1.0000	0035	0070	0105	0141	0176	0212	0247	0283	0319	6	12	18	24	30
46	1.0355	0392	0428	0464	0501	0538	0575	0612	0649	0686	6	12	18	25	31
47 48	1.0724	0761 1145	0799 1184	0837 1224	0875 1263	0913	0951	0990	1028	1067	6	13	19	25	32
49	1 1504	1544	1585	1626	1667	1303 1708	1343 1750	1383 1792	1423 1833	1463 1875	7	13 14	20 21	27 28	33
		1	-	1	i									1	34
50	1·1918 1·2349	1960 2393	2002	2045	2088	2131	2174	2218	2261	2305	7	14	22	29	36
51 52	1.2349	2846	2437	2482 2938	2527 2985	2572 3032	2617 3079	2662 3127	2708	2753	8	15	23	30	38
53	1.3270	3319	3367	3416	3465	3514	3564	3613	3175 3663	3222 3713	8	16 16	24 25	31 33	39 41
54	1 3764	3814	3865	3916	3968	4019	4071	4124	4176	4229	9	17	26	34	43
55	1.4281	4335	4388								1				
56	1.4826	4882	4388	4442 4994	4496 5051	4550 5108	4605 5166	4659 5224	4715 5282	4770 5340	10	18 19	27 29	36	45 48
57	1.5399	5458	5517	5577	5637	5697	5757	5818	5880	5941	10 10	20	30	38 40	48 50
58	1.6003	6066	6128	6191	6255	6319	6383	6447	6512	6577	11	21	32	43	53
59	1.6643	6709	6775	6842	6909	6977	7045	7113	7182	7251	11	23	34	45	56
60	1.7321	7391	7461	7532	7603	7675	7747	7820	7893	7966	12	24	36	48	60
61	1.8040	8115	8190	8265	8341	8418	8495	8572	8650	8728	13	26	38	51	64
62	1.8807	8887	8967	9047	9128	9210	9292	9375	9458	9542	14	27	41	55	68
63	1.9626	9711	9797	9883	9970	1	2.0145			2.0413	15	29	44	58	73
64	2.0503	0594	0686	0778	0872	0965	1060	1155	1251	1348	16	31	47	63	78
65	2.1445	1543	1642	1742	1842	1943	2045	2148	2251	2355	17	34	51	68	85
66	2.2460	2566	2673	2781	2889	2998	3109	3220	3332	3445	18	37	55	73	92
67	2.3559	3673	3789	3906	4023	4142	4262	4383	4504	4627	20	40	60	79	99
68	2.4751	4876	5002	5129	5257	5386	5517	5649	5782	5916	22	43	65	87	108
69	2.6051	6187	6325	6464	6605	6746	6889	7034	7179	7326	24	47	71	95	119
70	2.7475	7625	7776	7929	8083	8239	8397	8556	8716	8878	26	52	78	104	131
71	2.9042	9208	9375	9544	9714	9887	3.0061	3.0237	3.0415	3.0595	29	58	87		145
72	3.0777	9961	1146	1334	1524	1716	1910	2106	2305	2506	32	64	96	129	161
73	3.2709	2914	3122	3332	3544	3759	3977	4197	4420	4646	36		108		180
74	3.4874	5105	5339	5576	5816	6059	6305	6554	6806	7062	41	81	122	163	204
75	3.7321	7583	7848	8118	8391	8667	8947	9232	9520	9812	46	93	139	186	232
76	4.0108	0408	0713	1022	1335	1653	1976	2303	2635	2972	53	107	160	213	267
77	4.3315	3662	4015	4374	4737	5107	5483	5864	6252	6646					
78 79	4·7046 5·1446	7453 1929	7867 2422	8288 2924	8716 3435	9152 3955	9594 4486		5.0504 5578	5.0970			ifferei suffi		
				}				5026	1	6140			ccure		,
80	5.6713	7297	7894	8502	9124	9758	6.0405			6.2432	ĺ				
81 82	6.3138	3859	4596	5350	6122	6912	7720	8548	9395	7.0264					
82 83	7·1154 8·1443	2066 2636	3002 3863	3962 5126	4947 6427	5958 7769	6996 9152	8062	9158 9·2052	8.0285					
84		9.677	9.845	10.02	10.20	10.39		10.78	10.99	11.20					
				1							l				
85 86	11·43 14·30	11·66 14·67	11·91 15·06	12.16	12.43	12.71	13.00	13.30	13.62	13.95					
87	19.08	19.74	20.45	15·46 21·20	15·89 22·02	16·35 22·90	16·83 23·86	17·34 24·90	17·89 26·03	18·46 27·27					
88	28.64	30.14	31.82	33.69	35.80	38.19	40.92	44.07	47.74	52.08					
89	57.29	63.66	71.62	81.85	95.49	114.6	143.2	191.0	286.5	573.0					
90	œ		_												
				L				L		L					